

# Optimal Parameter Estimation of Permanent Magnet Synchronous Motor by Using Moth-Flame Optimization Algorithm

Abdolmajid Dejamkhooy, Sajjad Asefi

**Abstract**— Precision of model parameters is vital in a permanent magnet synchronous motor high performance and controllability. Since these parameters are affected by different operation conditions and load changes, then an accurate estimation strategy is quite necessary. In this paper, stator resistance and disturbed load torque, which assumed to be variable, are estimated. For this purpose, optimal parameter estimation problem is constructed as a least squares one. In the next step, the parameter identification as an optimization problem is solved by Moth-flame optimization, which is a novel nature-inspired heuristic algorithm. Simulation results and their comparison with Particle Swarm Optimization based method show high performance and good ability of the proposed method in PMSM parameter estimation.

**Index Terms**— Permanent magnet synchronous motor, Model parameter estimation, Moth-flame optimization, Particle swarm optimization

## I. INTRODUCTION

Recently, permanent magnet synchronous motors (PMSMs) have been widely used in high performance industrial applications, due to their high efficiency, high ratio of torque-to-inertia, suitable power factor, faster response and tough construction. The PMSMs have increasingly been utilized in electrical vehicles, aircraft, nuclear power stations, submarines, robotic applications, medical and industrial servo drives [1]. PMSMs can provide significant Performance improvement in many variable speed applications [2].

To provide fast and precise response, advanced control strategies require quick disturbance recovery, and parameter variations insensitivity. Accurate model construction for under study system is usually the important part in control system design [3]. In practical cases, the model parameters are not

known exactly and/or may vary slowly. This fact may be due to a variable operating point or a fault [4]. From this point of view, the parameter estimation can be divided into online and offline methods.

For linear systems, model parameter estimation is relatively easy task. However, the most practical systems show nonlinear behaviors. These nonlinearities are usually ignored. So, the linear system identification methods are applied to find approximate solution. However, they are inadequate in high-performance applications. Therefore, advanced approaches, which are specialized for nonlinear system identification, should be addressed [3].

So far, several methods have been presented to estimate the machine parameters of a permanent magnet synchronous machine. After applying voltage or current pulse to machine windings, the parameters have been calculated by using recorded data [5], [6]. These studies have not considered space harmonics. Thereby, a similar research has been presented, which focused on the harmonic effects and utilized Fast Fourier Transform (FFT) to calculate magnitude and phase of the fundamental harmonics [7]. Also, other signal processing methods such as Goertzel algorithm have been applied for this purpose [8]. The main disadvantage of these methods is that the parameters are estimated all at one in steady state. In other words, different operation conditions and load change effects are not considered in these methods. Other methods based on high carrier-frequency injection (CFI) technique, where the signal is superimposed onto the fundamental phase voltages, have been introduced [9–12]. The injection signal is usually a sinusoidal voltage. Therefore, it may cause acoustic noise, a motor current distortion, torque pulsation and large harmonic losses.

System identification methods have been widely employed to estimate PMSM parameters. Robust rotor position estimator based on the Sliding Mode Observer (SMO) has been proposed [13]. Also, Extended Kalman Filter (EKF) has been used to same purpose in sensorless PMSM [14]. Although, EKF method is less sensitive to the unknown measurement noise, but requires high computing capacity because of matrix calculations and particularly matrix inversions. Model reference adaptive system based mechanisms have shown good performance in the estimation of the parameters [1], [15]. A model reference based online identification method with its stability analysis and comparing with EKF has been

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developed in [4]. Despite expanded mathematical analysis, this method is seems too rough for practical applications.

Parameter estimation for a system with known model structure can be transferred to an optimization problem. The objective of the optimization problem is proximity of the system and model outputs. Therefore, the fitness function, which should be minimized, deals with difference between the real system and the estimated model outputs. On the other hand, evolutionary and swarm intelligence based algorithms are widely used to solve different types of optimization problems. Due to their advantages, they have been applied to model parameter estimation of PMSM. Particle Swarm Optimization (PSO) [3] and Differential Evolution (DE) [16] have been utilized for this purpose. Since these studies have been successful in PMSM parameter estimation, real-time implementation of the PSO based estimation has been investigated [17]. Afterward, the same methodology has been developed for fault diagnosis of PMSM [18].

In this paper, PSMS, which applied to a variable frequency drive system with cascaded PI controllers, is investigated. Stator resistance and disturbed load torque are estimated by the proposed method. Disturbed load torque is defined as summation of the actual load torque, and the disturbances caused by inertia and frictional coefficient. Indeed, stator resistance is directly related to motor operating temperature. Its value may increase to twice of its nominal value. Similarly, the rotor inertia and the frictional coefficient may vary as they are coupled with load torques of the motor. Unlike the more reviewed researches, these parameters are assumed to be variable depend on the motor operation conditions in this study. For this purpose, optimal parameter estimation problem is constructed as a minimizing problem. The fitness function is defined in the manner of summation of difference between state variable values of real and estimated systems. In the next step, the parameter identification as an optimization problem is solved by Moth-flame optimization, which is a novel nature-inspired heuristic algorithm. Simulation results and their comparison with PSO based method show high performance and good ability of the proposed method in PMSM parameter estimation.

The rest of the manuscript is organized as follows. In the next section, studied PMSM model and also parameter estimation strategy are described. A brief introduce to the Moth-flame optimization algorithm is expressed in section 3. Simulation results, comparisons and discussions are presented in the section 4. Finally, the section 5 gives a conclusion of the paper.

## II. PMSM MODEL AND ESTIMATION STRATEGY

### A. Model description

The two-axis dq-model is the most commonly used model for variable speed PMSM drive control studies. PMSM is described by nonlinear differential equations. The system of nonlinear equations can be divided into two subsystems, i.e. electrical and mechanical system. The electrical system in rotating reference frame is as

$$\frac{di_d^r}{dt} = \frac{1}{L_d} [v_d^r - R_s i_d^r + \omega_r L_q i_q^r] \quad (1)$$

$$\frac{di_q^r}{dt} = \frac{1}{L_q} [v_q^r - R_s i_q^r - \omega_r L_d i_d^r - \omega_r \psi_{mag}] \quad (2)$$

where  $i_{dr}$ ,  $i_{qr}$ ,  $v_{dr}$ , and  $v_{qr}$  are the dq-components of the stator currents and voltages;  $\omega_r$  is the rotor electrical angular speed; parameters  $R_s$ ,  $L_q$ ,  $L_d$  are the stator resistance, d-axis and q-axis inductance, and  $\psi_{mag}$  is the permanent magnet flux linkage.

The mechanical system includes two equations, which deal with Newton's law and produced electromechanical torque as

$$\frac{d\omega_r}{dt} = n_p \frac{1}{J} \left[ T_e - B \frac{\omega_r}{n_p} - T_L \right] \quad (3)$$

$$T_e = \frac{3}{2} n_p \left[ i_q^r \psi_{mag} + (L_d - L_q) i_d^r i_q^r \right] \quad (4)$$

$i_{dr}$ ,  $i_{qr}$  and  $\omega_r$  are taken as the state variables/outputs. Also,  $v_{dr}$  and  $v_{qr}$  are chosen as control signals/inputs. Other parameters and coefficients are usually adopted as constant values. This assumption causes to inaccuracy in high performance applications and advanced control schedules. In practice, PMSM operates under various operating conditions, where different disturbances and parameter variations are unavoidable and immeasurable. For example,  $J$  and  $B$  vary by changing load level. Similarly,  $R_s$ , which is directly related to temperature, may rise to twice of its nominal value. Therefore, precise model parameter estimation strategy is required to achieve a successful tracking and control of PMSM.

### B. Parameter estimation strategy

As the system model is known but the parameters are unknown, this parameter identification problem can be treated as an optimization problem. The main idea is comparison of the main and the estimated system outputs. The difference between the output values is considered as an index to make the objective function, which should be minimized by the heuristic algorithm. In other words, the best solution is accrued when the fitness function value is minimum. This ideal condition deals with matching the outputs. The structure of the parameter estimation approach is demonstrated in Figure 1.

It is clear that the estimated model has the same structure of the main system. Also, same input signal is fed into the both systems.  $P$  is defined as vector of the undetermined parameters, which should be estimated i.e.  $\hat{P}$ . Stator resistance ( $R_s$ ) and disturbed load torque ( $T_{Ld}$ ) are parameters which estimated in this study. Therefore  $P$  can be constructed as  $P = [R_s \ T_{Ld}]^T$ .

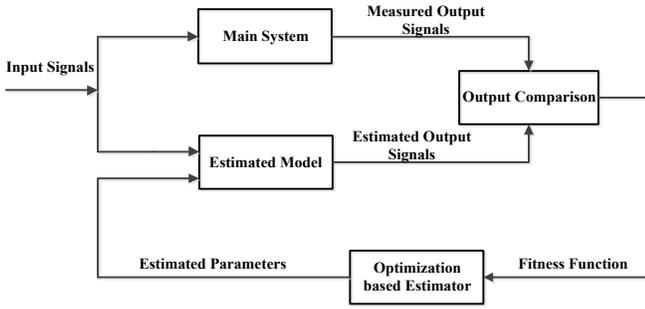


Fig. 1. Block diagram of the parameter estimation strategy

In fact,  $J$  and  $B$  appear in  $T_{Ld}$ . Disturbed load torque is the summation of the actual load torque ( $T_L$ ), and the disturbances caused by inertia and frictional coefficient variations, as

$$T_{Ld} = T_L + \tilde{J} \frac{1}{n_p} \frac{d\omega_r}{dt} + \tilde{B} \frac{1}{n_p} \omega_r \quad (5)$$

where  $\tilde{J} = J - J_0$  and  $\tilde{B} = B - B_0$ .  $J_0$  and  $B_0$  denote the nominal values of motor inertia and viscous friction coefficient.

To find out the unknown parameters the output of the systems are compared. If  $y$  and  $\hat{y}$  denote main and estimated system outputs respectively, a fitness or cost function can be defined to transform the parameter identification problem to an optimization problem. The function may be considered as the weighted quadratic function which is defined as follows

$$C(\hat{p}) = \int_t (y - \hat{y})^T W (y - \hat{y}) dt \quad (6)$$

where  $y = [i_{abc} \ \omega_r]^T$  and  $W$  is a positive matrix as weighted factor.

It is worth to mention that eventually the fitness function depends on the parameters which will be estimated. In other words, by minimizing the fitness function, the optimum values for the parameters are yields.

For this investigation (6) is rewritten as

$$C(\hat{R}_s, \hat{T}_{Ld}) = \sum_{k=1}^n \left[ \begin{array}{l} (i_a(k) - \hat{i}_a(k))^2 + (i_b(k) - \hat{i}_b(k))^2 \\ + (i_c(k) - \hat{i}_c(k))^2 + w (\omega_r(k) - \hat{\omega}_r(k))^2 \end{array} \right] \quad (7)$$

where  $i_{abc}$  and  $\omega_r$  are phase currents and rotor speed of the main system (outputs of the main system), while  $\hat{i}_{abc}$  and  $\hat{\omega}_r$  are the output values for the estimated system.  $R_s$  and  $T_{Ld}$  are the unknown parameters which are going to be identified, and  $W$  is the weighting factor that has been assumed as ratio of stator current magnitude to rotor speed magnitude.

To minimize the fitness function and yield the optimized parameter values, moth-flame optimization algorithm is utilized. It is a novel nature-inspired heuristic method which has shown high ability in solving rough optimization problems [19]. Also, the problem is accomplished and compared by PSO method. In the next section, a brief introduce to moth-

flame optimization algorithm is presented.

### III. MOTH-FLAME OPTIMIZATION ALGORITHM

Recently, a new swarm intelligence based algorithm known as Moth Flame Optimization Algorithm (MFOA) has been developed [19]. The inspiration source of the algorithm is the lateral movement of moths around a bright object such as candle, which is found in nature. Moths have a special movement mechanism i.e. transverse orientation. This ability helps them to fly at night. To this aim, they keep a fixed angle with respect to moon. In order to move in a straight line, this method is very helpful, considering that light source is far away. If the moths be closer to the light source, again they will try to keep a constant angle regarding this light source. Since, the distance between them is not far enough, it results a spiral movement of moths around the candle. Finally, after a few rounds they will converge to light source.

In MFO algorithm moths and flames play the main roles and both of them are considered as a result for this algorithm. In each iteration, their update mechanism is different. Moths are the search agents. They contain values of the problem's parameters. Flames are the best position of moths throughout the search space. In other words, moths pin the best obtained solution by using flames. So, each moth flies through the search space, finds solutions and updates itself. The set of moths can be presented as

$$M = \begin{bmatrix} m_{1,1} & m_{1,2} & \cdots & \cdots & m_{1,d} \\ m_{2,1} & m_{2,2} & \cdots & \cdots & m_{2,d} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ m_{n,1} & m_{n,2} & \cdots & \cdots & m_{n,d} \end{bmatrix} \quad (8)$$

where  $n$  is the number of moths and  $d$  is the number of variables. Also, the fitness values for all the moths are stated as

$$OM = \begin{bmatrix} OM_1 \\ OM_2 \\ \vdots \\ OM_n \end{bmatrix} \quad (9)$$

Flames and their corresponding fitness function values can be stored as

$$F = \begin{bmatrix} F_{1,1} & F_{1,2} & \cdots & \cdots & F_{1,d} \\ F_{2,1} & F_{2,2} & \cdots & \cdots & F_{2,d} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ F_{n,1} & F_{n,2} & \cdots & \cdots & F_{n,d} \end{bmatrix} \quad (10)$$

and



TABLE I  
NOMINAL VALUE OF THE PMSM PARAMETERS

Parameter	Nominal values
Power rating $P_r$	19.8 (kW)
Rated rotor speed	1700 (rpm)
Current at rated speed $I_r$	41.56 (A)
Torque at rated speed $T_r$	67.27 (N m)
Voltage constant $k_e$	1.33 (V s/rad)
Torque constant $k_t$	1.629 (N m/A)
Max bus voltage $V_{DC}$	560 (V)
Pole pairs $n_p$	4
Stator resistance $R_s$	0.17 ( $\Omega$ )
q-axis inductance $L_q$	1.9 (mH)
d-axis inductance $L_d$	1.9 (mH)
Static friction $T_f$	0.1483 (N m)
Damping coefficient $B$	0.00115 (N m s/rad)
Moment of inertia $J$	0.008 (kg m <sup>2</sup> )

In each generation of MFOA, number of moths and constant for announcing the shape of the logarithmic spiral there are set 100 and 1, respectively. The optimization process of the fitness function by MFOA and PSO is shown in Figure 3 and the final value of fitness function for both optimization techniques is provided in Table 2.

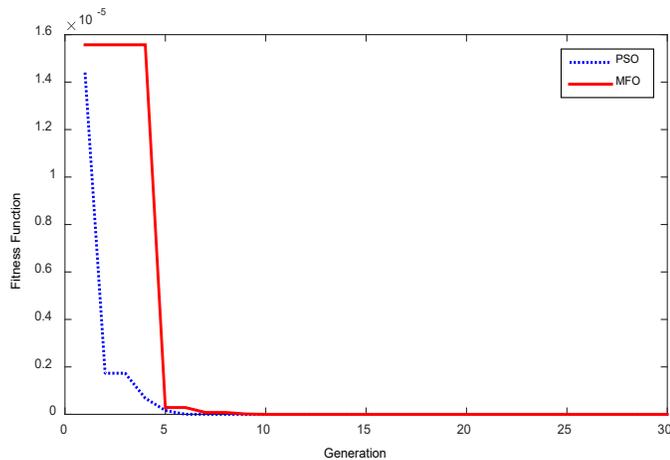


Fig. 3. Fitness function optimization process

TABLE II Final value of fitness function		
Algorithm	PSO	MFO
Final fitness value	0.2874e-9	0.0013e-9

The stator resistance estimation process is shown in Figure 4. MFOA based method converged after less than 25 iterations. The resulted value is 0.173  $\Omega$ , which has 1.76% deviation from actual value. Although PSO based method converges faster than MFO, but its calculated value for stator resistance is 0.33  $\Omega$ . Therefore, the MFOA based proposed method is more accurate than PSO ones. As demonstrated in Figure 5, disturbed load torque by the methods converges to 2.99 Nm. According to actual value of  $T_{Ld}$  i.e. 3 Nm, estimation error is 0.33%. According to these error values, these estimations can be adopted as high precision.

So far estimation has been conducted for one set of data. In other words, an offline or static estimation has been performed. If the number of iteration for both methods set 30,

then meeting accurate results will be guaranteed. The same estimation strategy can be developed to online parameter identification. For online identification, the measured data are sent to the proposed estimator as input. When the algorithms finish searching for 30 iterations, the identification process will be terminated. For each round of the applying algorithms, the previously obtained optimum parameters are used as the initial values for next round. This will result in faster convergence in the case of online application of the method. The entire optimization process of MFO and PSO algorithms during online optimization are shown in Figure 6. According to this demonstration, it is obvious that the algorithms converge within 10 to 15 iterations whether starts with a good or bad guess. The main reason of different starting fitness value is that when system parameter changes, i.e. the system operating point changes, the fitness will have different sensitivity. So, there might be a large change in fitness while there is a small change in parameters.

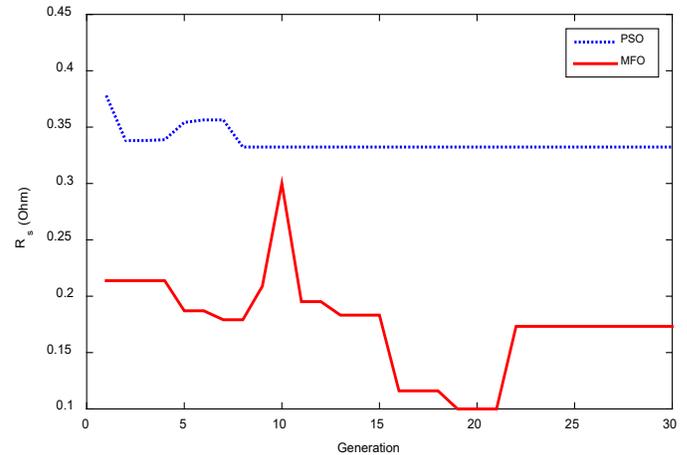


Fig. 4. Estimation of the stator resistance

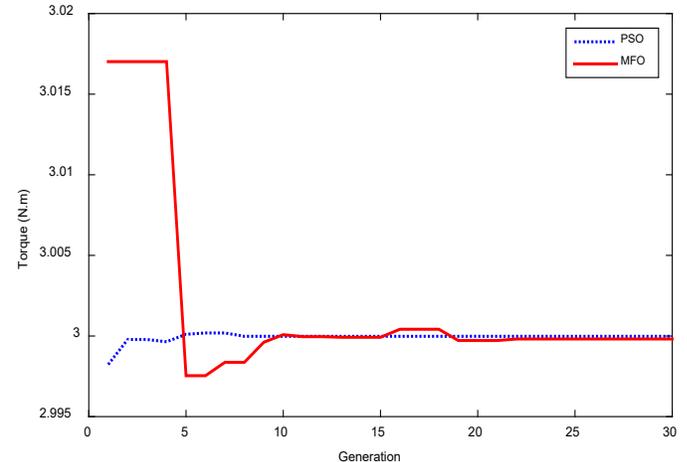


Fig. 5. Estimation of the torque

After comparing the actual and identified parameters, the performance of the main and estimated systems are compared. As mismatching the estimated parameters, may cause system dynamic response deviation, so, this investigation is essential.

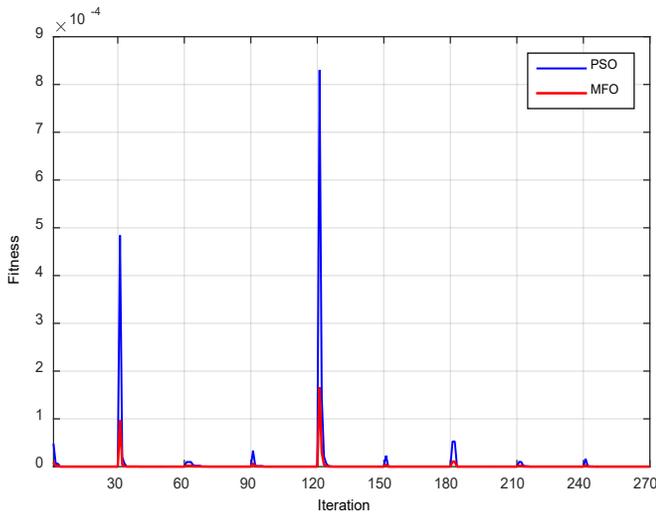


Fig. 6. Fitness function optimization process during online estimation

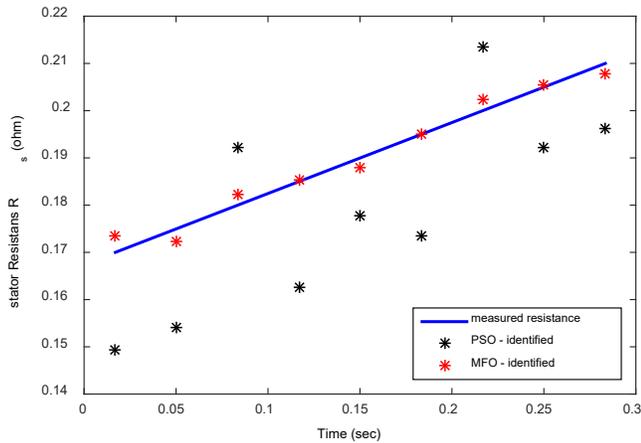


Fig. 7. Online estimation of stator resistance

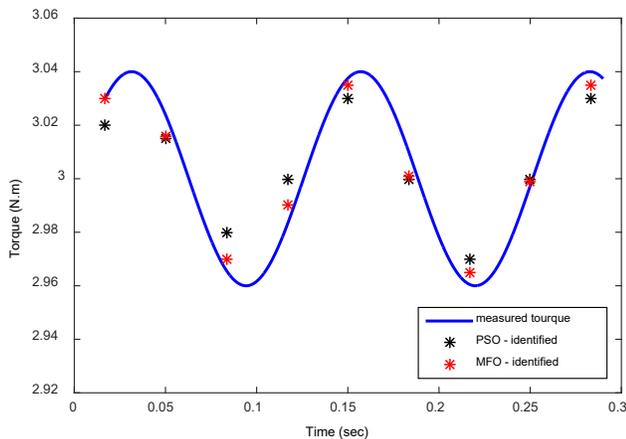


Fig. 8. Online estimation of load torque

The results are illustrated in Figure 9 and 10. First plot shows the stator phase current  $i_a$  and the next one is the rotor angular speed. Since the performances of the two models match each other quite well.

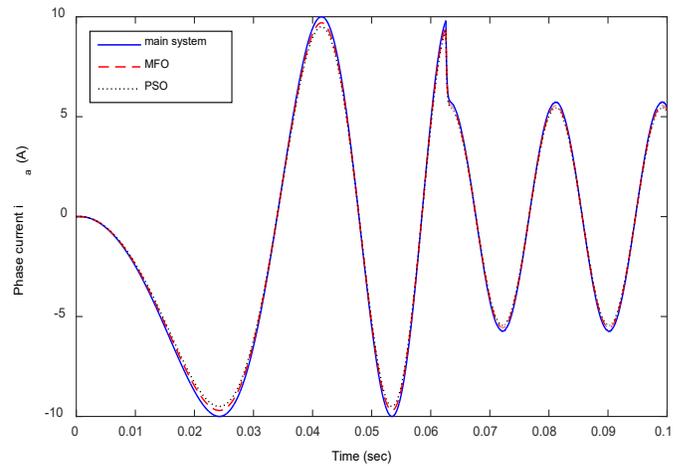


Fig. 9. Phase current ( $i_a$ ) as performance index of the models

In this paper, the convergence has been presented in term of iteration number for the algorithms. The simulations continue for 30 iterations.

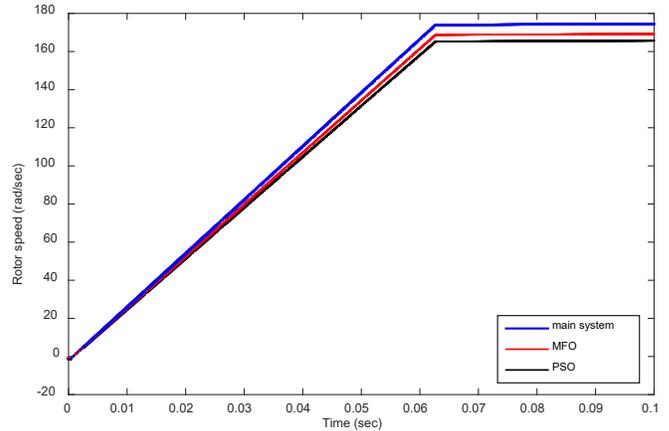


Fig. 10. Rotor speed ( $\omega_r$ ) as performance index of the models

The simulations for present period will continue until the 30 iterations complete and after that the next period of simulation will start. In other words, time has been not used for analyzing the algorithm performances. It worth noting that, the speed of computations is highly impacted by factors such as applied hardware, the sampling frequency, and other computer properties. As mentioned before, if we apply previous optimum results for the next period, we can save lots of time in continuous online applications.

### V. CONCLUSION

In this paper, to estimate PMSM nonlinear model parameters, a method based on MFOA has been proposed. Simulation results show that the proposed estimator can approximate the parameters in both online and offline modes high precisely. The estimation error values have been resulted around 1%, which confirms the method performance. Also, the estimated system can track the actual one successfully. Since the presented method show a high performance potential in identifying when the parameters are subjected to an uncertainties or a fault. Therefore, it can be applied as fault diagnosis system using the parameter variations as fault

symptoms. This optimization based identification method, although applied to PMSM, but is generally applicable to other systems with complicated nonlinear model structure.

## REFERENCES

- [1] A. Khlaief, *et al.*, "A MRAS-Based Stator Resistance and Speed Estimation for Sensorless Vector Controlled IPMSM Drive," *Electric Power System Research*, vol. 108, pp. 1-15, 2014.
- [2] J. Jang, *et al.*, "Design of a Variable-Flux Permanent-Magnet Synchronous Motor for Adjustable-Speed Operation," *IEEE Transactions on Industry Applications*, vol. 52, pp. 2996 - 3004, July-Aug. 2016.
- [3] L. Liu, *et al.*, "Particle Swarm Optimization-Based Parameter Identification Applied to Permanent Magnet Synchronous Motors," *Engineering Applications of Artificial Intelligence*, vol. 21, pp. 1092–1100, 2008.
- [4] T. Boileau, *et al.*, "Online Identification of PMSM Parameters: Parameter Identifiability and Estimator Comparative Study," *IEEE Transactions on Industry Applications*, vol. 47, pp. 1944 - 1957, July-Aug. 2011.
- [5] G. Stumberger, *et al.*, "Evaluation of Saturation and Cross Magnetization Effects in Interior Permanent Magnet Synchronous Machine," *IEEE Transactions on Industry Applications*, vol. 39, pp. 1264–1271, Sep-Oct. 2003.
- [6] G. Franceschini, *et al.*, "Impact of Cross Saturation in Synchronous Reluctance Motors of the Transverse-laminated Type," *IEEE Transactions on Industry Applications*, vol. 36, pp. 1039–1046, Jul-Agu. 2000.
- [7] K. M. Rahman, and S. Hiti, "Identification of Machine Parameters of Synchronous Motor," *IEEE Transactions on Industry Applications*, vol. 41, pp. 557 - 565, March-April. 2005.
- [8] J. Yoon, *et al.*, "Off-Line Parameter Identification of Permanent Magnet Synchronous Motor Using a Goertzel Algorithm," *Journal of Electrical Engineering Technology*, vol. 10, pp. 2262-2270, 2015.
- [9] N. Bianchi, *et al.*, "Comparison of PM Motor Structures and Sensorless Control Techniques for Zero-Speed Rotor Position Detection," *IEEE Transactions on Power Electronics*, vol. 22, pp. 2466 - 2475, Nov. 2007.
- [10] J. Hu, *et al.*, "Eddy Current Effects on Rotor Position Estimation and Magnetic Pole Identification of PMSM at Zero and Low Speeds," *IEEE Transactions on Power Electronics*, vol. 23, pp. 2565–2575, Sept. 2008.
- [11] D. Raca, *et al.*, "Carrier-Signal Selection for Sensorless Control of PM Synchronous Machines at Zero and Very Low speeds," *IEEE Transactions on Industry Applications*, vol. 46, pp. 167–178, Jan-Feb. 2010.
- [12] A. Yoo and K.S. Sul, "Design of Flux Observer Robust to Interior Permanent-Magnet Synchronous Motor Flux Variation," *IEEE Transactions on Industry Applications*, vol. 45, pp. 1670–1677, Sept-Oct. 2009.
- [13] M.S. Islam, *et al.*, "Design and Performance Analysis of Sliding Mode Observers for Sensorless Operation of Switched Reluctance Motors," *IEEE Transactions on Control Systems Technology*, vol. 11, pp. 383 - 389, May 2009.
- [14] M. Boussak, "Implementation and Experimental Investigation of Sensorless Speed Control with Initial Rotor Position Estimation for Interior Permanent Magnet Synchronous Motor Drive," *IEEE Transactions on Power Electronics*, vol. 20, pp. 1413–1422, Nov. 2005.
- [15] L. Liu and D. A. Cartes, "Synchronization Based Adaptive Parameter Identification for Permanent Magnet Synchronous Motors," *IET Control Theory & Applications*, vol. 1, pp. 1015 – 1022, July 2007.
- [16] G. Lin, *et al.*, "Parameter Identification of PMSM Using Immune Clonal Selection Differential Evolution Algorithm," *Mathematical Problems in Engineering*, vol. 2014, pp. 1-10 pages, 2014.
- [17] W. Liu, *et al.*, "Real-Time Particle Swarm Optimization Based Parameter Identification Applied to Permanent Magnet Synchronous Machine," *Applied Soft Computing*, vol. 11, pp. 2556-2564, 2011.
- [18] W. Liu, *et al.*, "Modeling and Detecting the Stator Winding Fault of Permanent Magnet Synchronous Motors," *Simulation Modelling Practice and Theory*, vol. 27, pp. 1-16, 2012.
- [19] S. Mirjalili, "Moth-Flame Optimization Algorithm: A Novel Nature-Inspired Heuristic Paradigm," *Knowledge-Based Systems*, vol. 89, pp. 228-249, 2015.



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